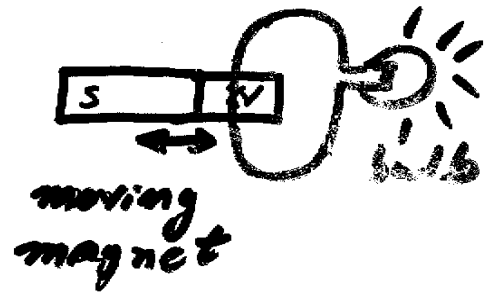


# ELECTROMAGNETISM

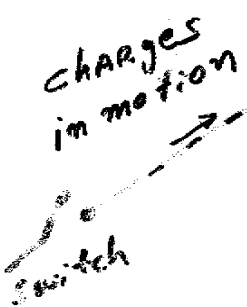
PH: 222



**FARADAY:**  
moving magnet  
produces current



• 1820 Oersted:  
charges in motion  
produce wire magnetism

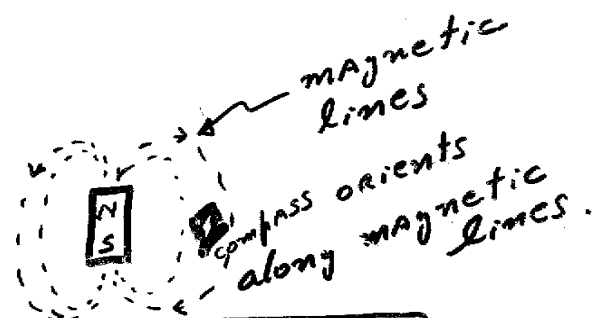


compass  
changes orientation  
upon closing the  
switch

• Electrostatic



ELECTRICITY



MAGNETISM

2

# ELECTROMAGNETISM



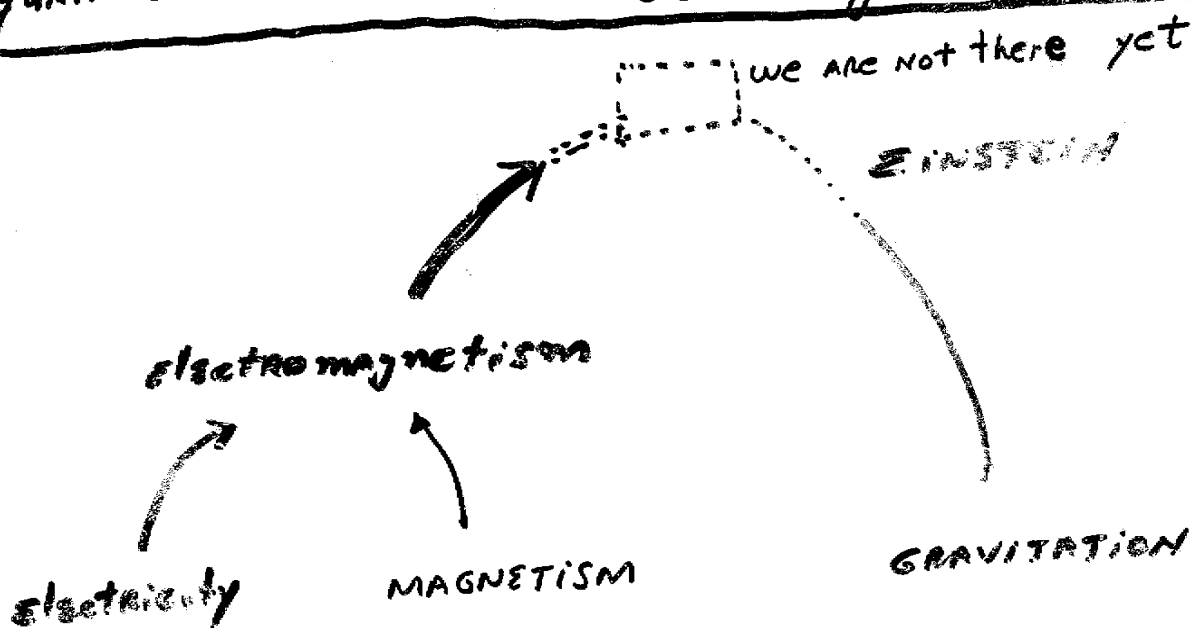
MAXWELL  
EQUATIONS

$$\vec{E} = \vec{E}(\vec{B}, \frac{d\vec{B}}{dt})$$

$$\vec{B} = \vec{B}(\vec{E}, \frac{d\vec{E}}{dt})$$

Theoretical  
foundation

MAXWELL equations PREDICTS that light is an electromagnetic wave



3

CLASSICAL MECHANICS  
(Newton's laws)

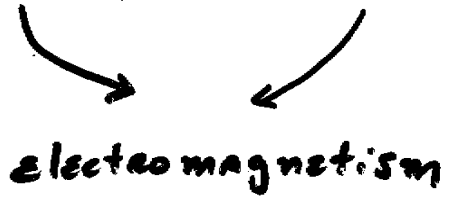
NO valid in  
the micro-  
world.



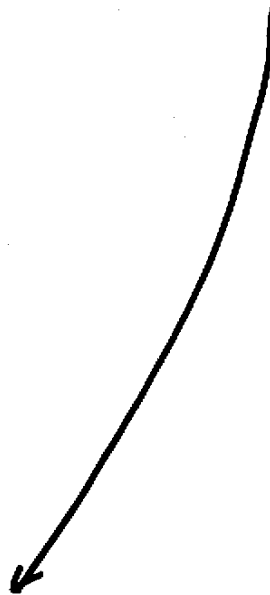
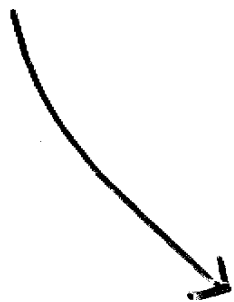
QUANTUM MECHANICS

ELECTRICITY

MAGNETISM

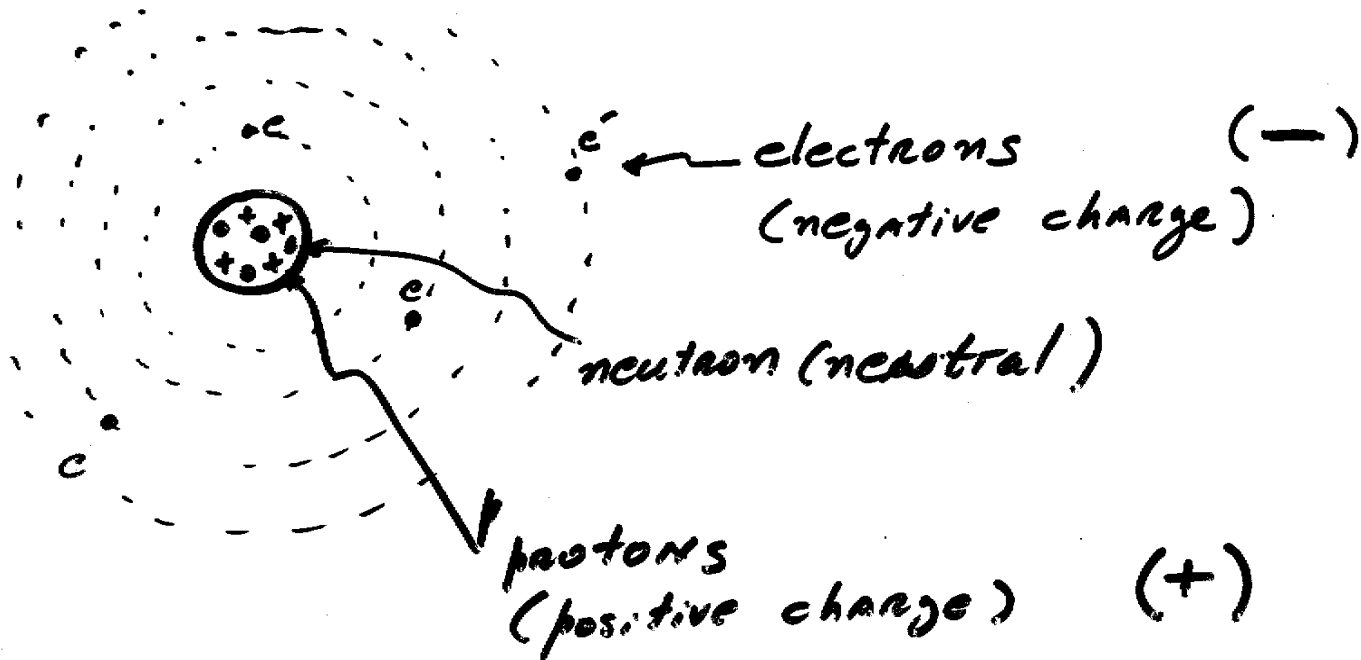


electromagnetism



QUANTUM ELECTRODYNAMICS

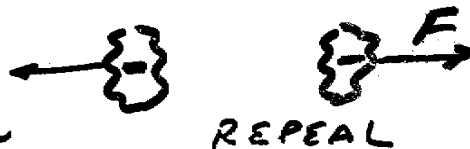
## ELECTRIC CHARGE



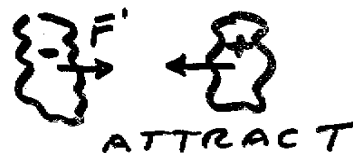
Typically: ATOMS ARE ELECTRICALLY NEUTRAL

$$\#e = \#p$$

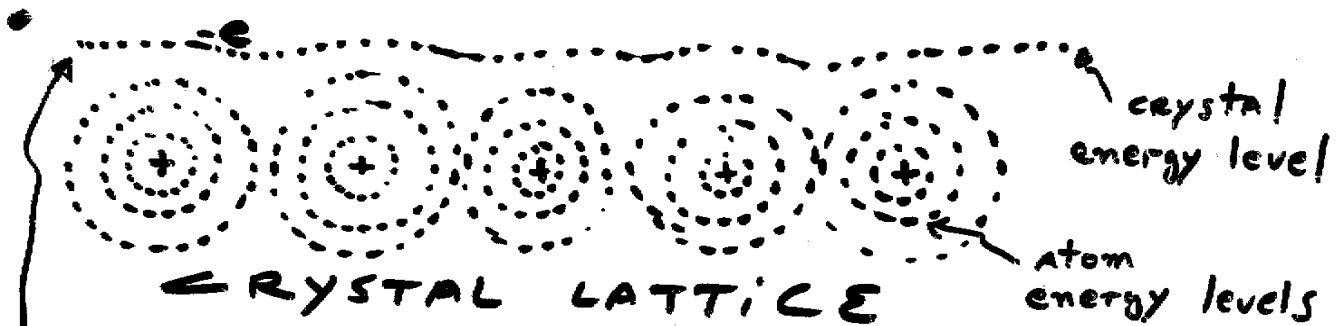
- Charges of the SAME sign REPEL each other



- Charges of OPPOSITE sign ATTRACT each other



## 6 CONDUCTORS (contain "free electrons")



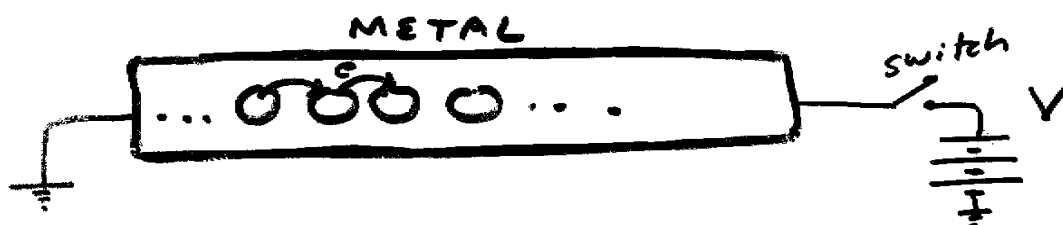
electrons in the crystal energy level are "FREE" to wander across the metal

In short, we may say:



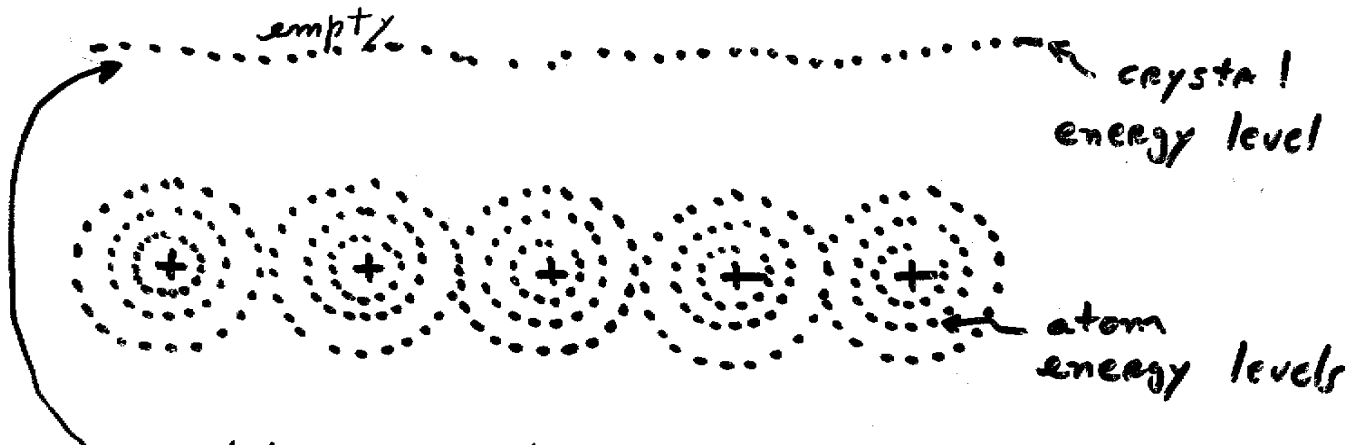
CONDUCTOR is a neutral structure with electrons FREE to move across the whole crystal.

Another classical view



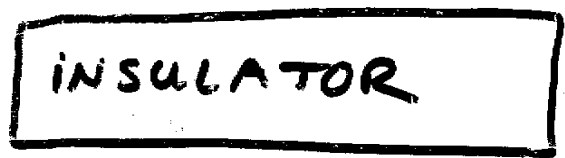
Q: How fast electrons jump from atom to atom?  $10^6$  m/s, 10 m/s,  $10^6$  m/s?

# INSULATORS (do not have free electrons)

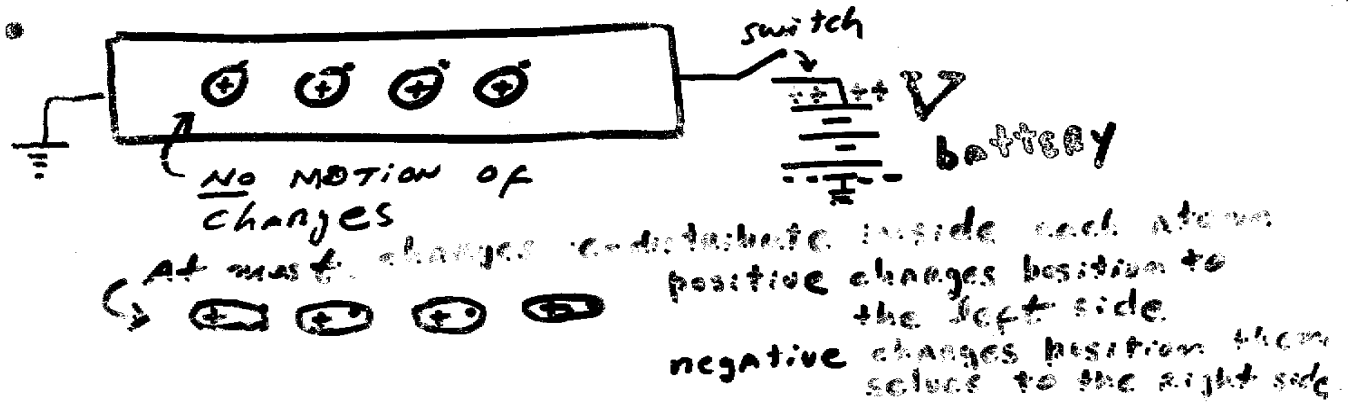


insulators do not have free electrons in the crystal energy level

• WE CAN SAY:



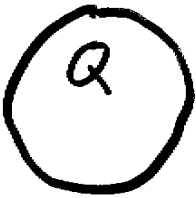
NO FREE electrons available



(For really high voltage  $V$ , we may destroy the material)

8

• CHARGE IS QUANTIZED



charge  $Q$

$$Q = Ne$$

$$N = \pm 1, \pm 2, \pm 3, \dots$$

$$e = 1.6 \times 10^{-19} \text{ coulomb}$$

$e$  is the smallest charge that has been detected.

(It has never been detected charges

like  $0.25e$  nor any fraction of  $e$

detected charge  $Q = 0.37e \leftarrow \text{WRONG!} \right)$

# Phenomenon of INDUCED CHARGE

## Example

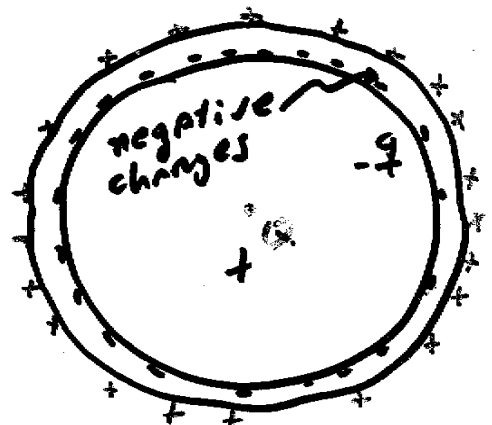
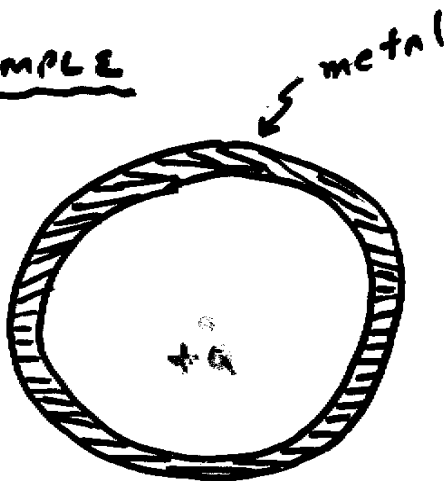


METAL  
(NEUTRAL)



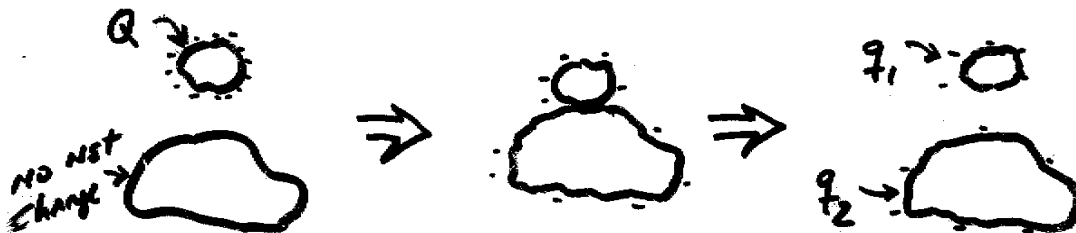
Net force

## EXAMPLE



10

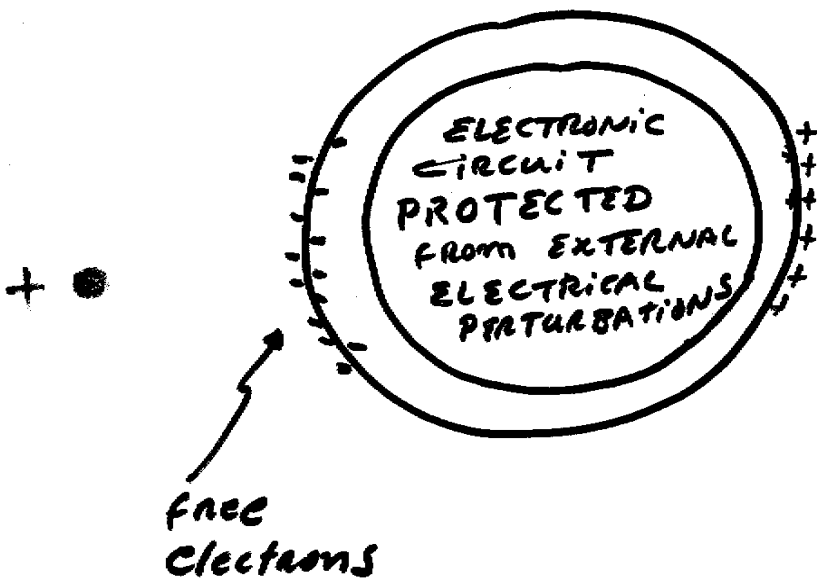
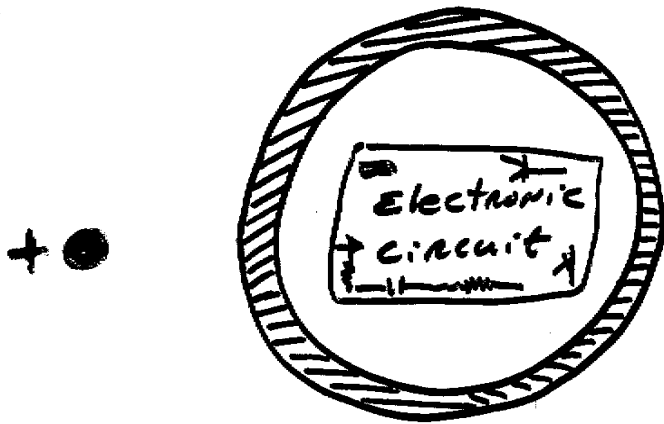
• CHARGE IS CONSERVED



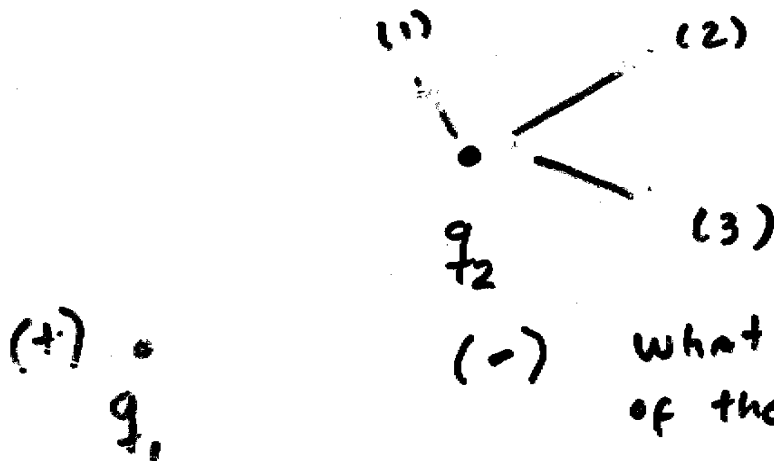
$$\underbrace{Q}_{\text{before}} = \underbrace{q_1 + q_2}_{\text{after}}$$

• SAMPLE PROBLEM 22-3, TEXTBOOK p. 513

" EXAMPLE

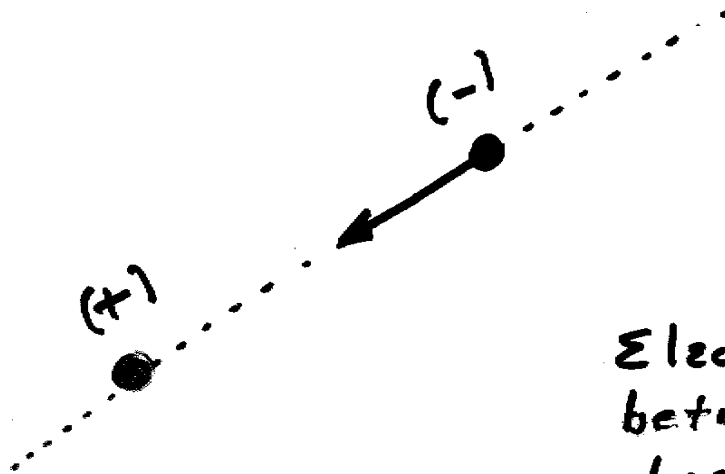


# COULOMB'S LAW



What is the direction of the force acting on the charge  $q_2$ ?

ANSWER:



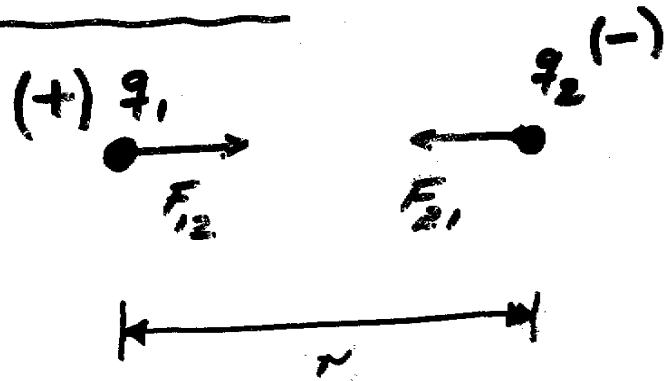
Electrical force between two charges acts along the line that passes through the charges

- 13 Reading homework: - induction (page 508, textbook)  
 - semiconductors  
 - superconductors

## QUANTITATIVE ASPECT

• We know

$$\vec{F}_{12} = -\vec{F}_{21}$$



what is new is  
 the following

$r$ : distance between the  
 particles 1 and 2

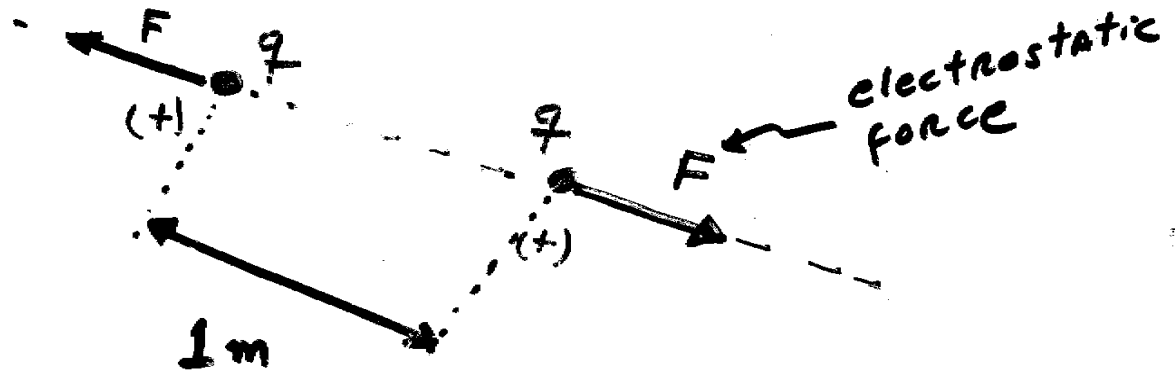
$$|\vec{F}_{12}| = \left( \frac{1}{4\pi\epsilon_0} \right) \frac{|q_1||q_2|}{r^2} \quad \text{Coulomb's law}$$

where  $\frac{1}{4\pi\epsilon_0} = 9 \times 10^9 \text{ N}\cdot\text{m}^2/\text{C}^2 = k$

$$\epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2/\text{N}\cdot\text{m}^2$$

## Definition of the unit charge: THE COULOMB

If the distance between two punctual  
charges is 1 meter,



and  $F = 9 \times 10^9$  Newtons

then

$$q = ?$$

15

• When  $q_1 = q_2 = 1$  coulomb and they are apart  $r = 1$  meter, the electrostatic force they exert each other is  $9 \times 10^9$  Newtons

definition of the unit charge:  
the coulomb (C)

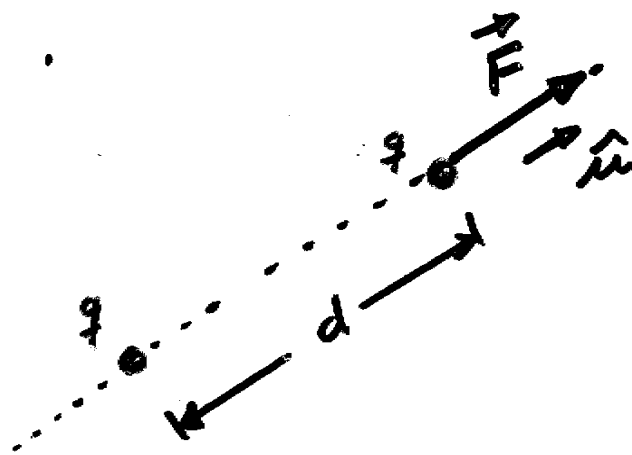
16

## FORCE is a VECTOR

- Remember: the electrostatic force is a VECTOR !

So, we must provide magnitude and orientation

17



$\vec{F}$  = magnitude & orientation

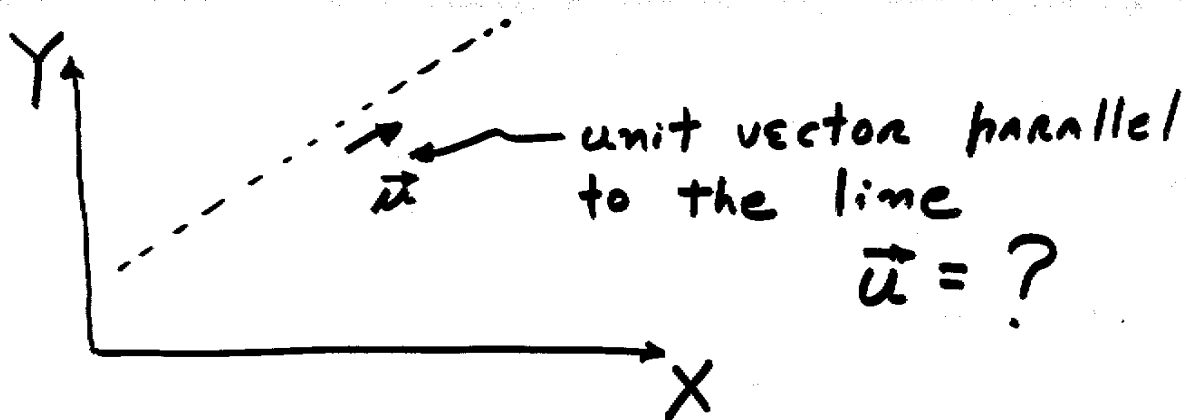
$$= F \hat{u} \quad F \equiv |\vec{F}|$$

unit vector

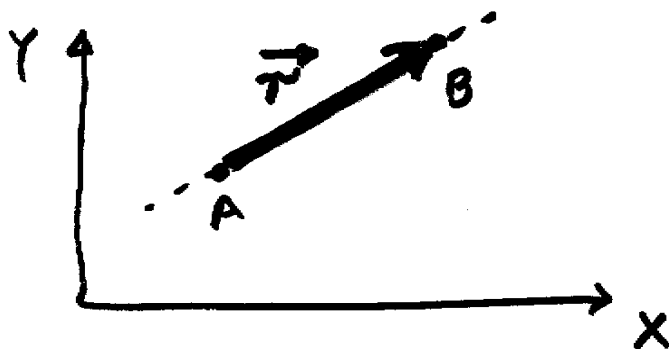
$$9 \times 10^9 \frac{q^2}{d^2}$$

We know how to evaluate the magnitude  
but  
how to figure out the unit vector?

18



- ① Pick up any two points **A** and **B** along the line



- ② Define the vector  $\vec{r}$   
 Evaluate the magnitude of  $\vec{r}$ :  $r = |\vec{r}|$

- ③ The vector  $\frac{\vec{r}}{|\vec{r}|}$  will be a unit vector along the specified line.  $\vec{u} = \frac{\vec{r}}{|\vec{r}|}$

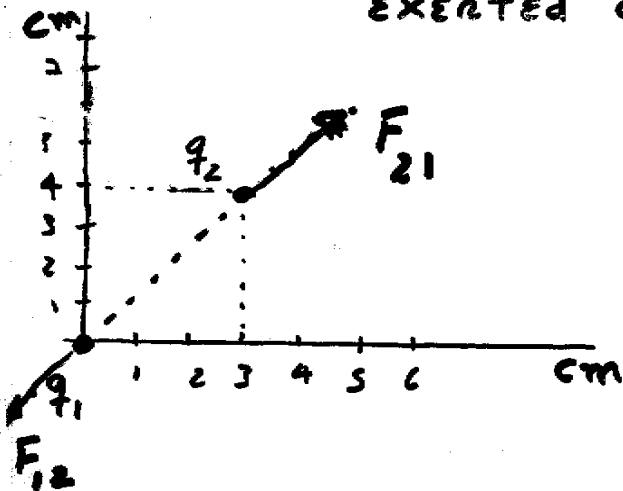
19 Exercise

Find the electrostatic FORCE  
EXERTED on charge  $q_2$  due to

the charge  $q_1$ .

$$q_1 = 10 \mu\text{C}$$

$$q_2 = 5 \mu\text{C}$$

SOLUTION

a) Magnitude of the force

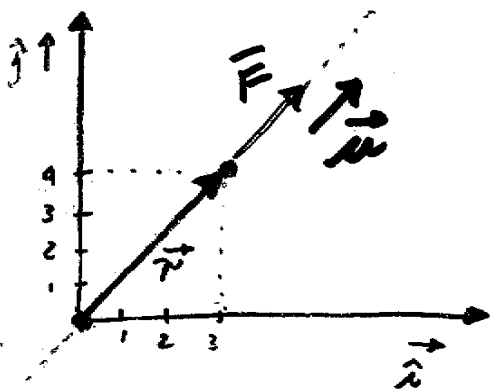
$$F = |\vec{F}| = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r^2} = 9 \times 10^9 \frac{\text{Nm}^2}{\text{C}^2} \frac{50 \times 10^{-12} \text{C}^2}{(5 \text{cm})^2}$$

$\leftarrow 10^{-2} \text{m}$

$$\boxed{F = 180 \text{ N}}$$

$$\vec{F} = 180 \hat{\mu}$$

b) Orientation of the force  
strategy  $\rightarrow$  let's find the proper  
UNIT VECTOR



$$\vec{r} = 3\hat{i} + 4\hat{j} \quad \text{cm}$$

$$|\vec{r}| = \sqrt{3^2 + 4^2} = 5 \quad \text{cm}$$

unit  
vector

$$\boxed{\vec{u} = \frac{\vec{r}}{|\vec{r}|} = \frac{3}{5}\hat{i} + \frac{4}{5}\hat{j}}$$

20

The answer to the problem is:

$$\vec{F} = F \vec{u} = 180 \text{ N } \vec{u} \quad (1)$$

$\uparrow$                      $\uparrow$   
 magnitude          unit  
    vector

Equally acceptable is the following answer:

$$\begin{aligned} \vec{F} &= 180 \text{ N} \cdot \left( \frac{3}{5} \hat{i} + \frac{4}{5} \hat{j} \right) \\ &= 108 \hat{i} + 144 \hat{j} \quad (2) \\ &\quad \text{Newtons} \quad \text{Newtons} \end{aligned}$$

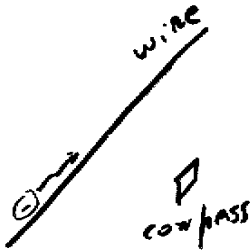
EXERCISE Just for the sake of verifying we are doing things all right, FIND the magnitude of the vector force  $\vec{F}$  given by expression (2)

# Review

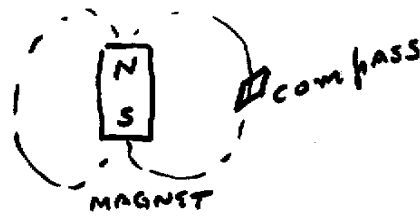
## ELECTROSTATIC



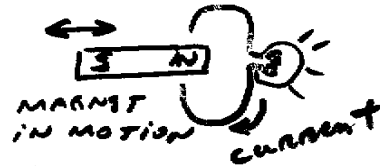
Charges in motion produces magnetism



## MAGNETISM



MAGNETS in motion produces electric current



Electricity and MAGNETIC phenomena are governed by the same physical laws

## ELECTROMAGNETISM

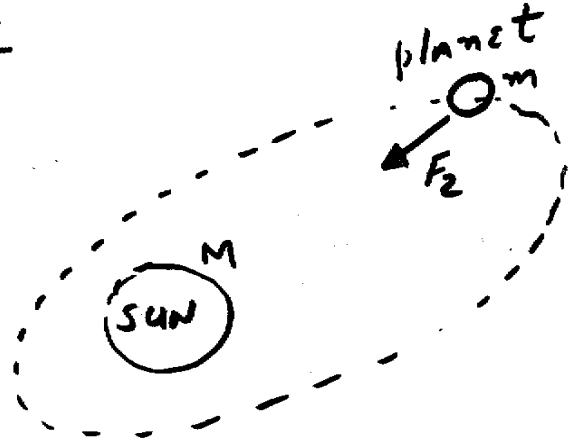
# THE 4 FORCES IN NATURE

- 2
- p • +
- e • -
- n • zero charge



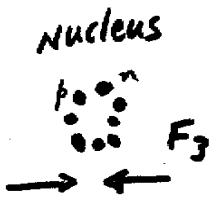
Electromagnetic force

(1)



Gravitational force

(2)

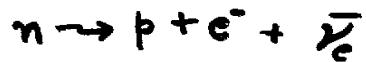


strong force

(3)

(keep nucleons together stronger than electromag force) shorter range than "

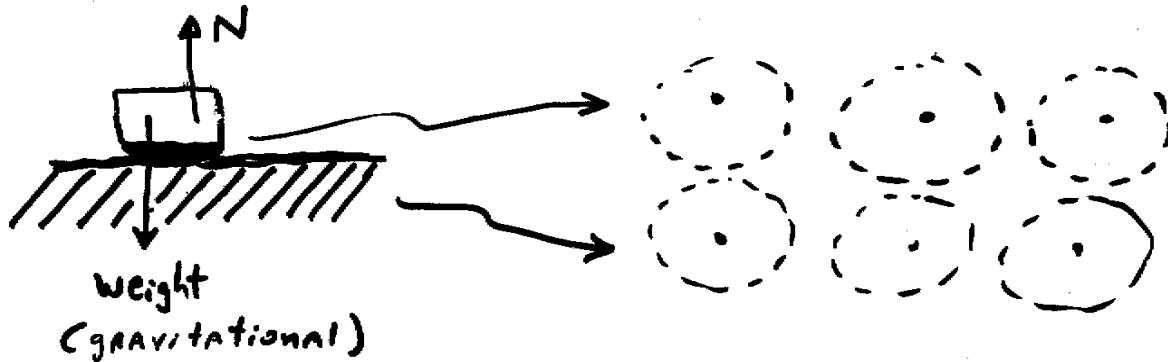
nucleus



WEAK force

(4)

# NORMAL FORCE (electromagnetic)



---

## Reading Assignment

- sample problem 22-4 page 515
- sample problem 22-3 page 513

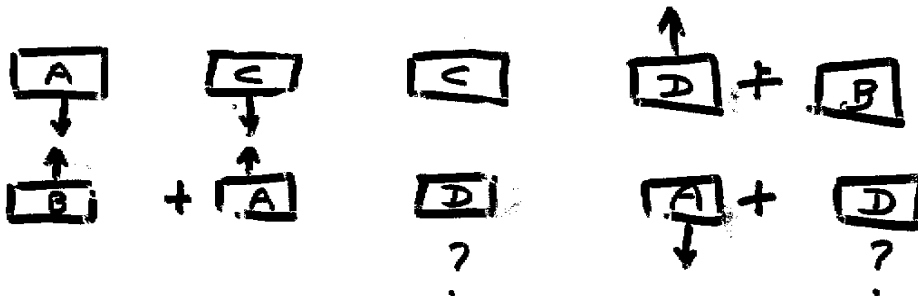
## Suggested practice problems

Chapter 22: 2E, 8P, 15P, 23E

## \* Applications

- Electrostatic paint spraying
- Powder coating
- Non impact ink-jet printing
- Photocopying

EXERCISE (page 508 textbook)



Repel or attract each other?

A charged plastic plate

B "

D "

C electrically neutral copper plate.

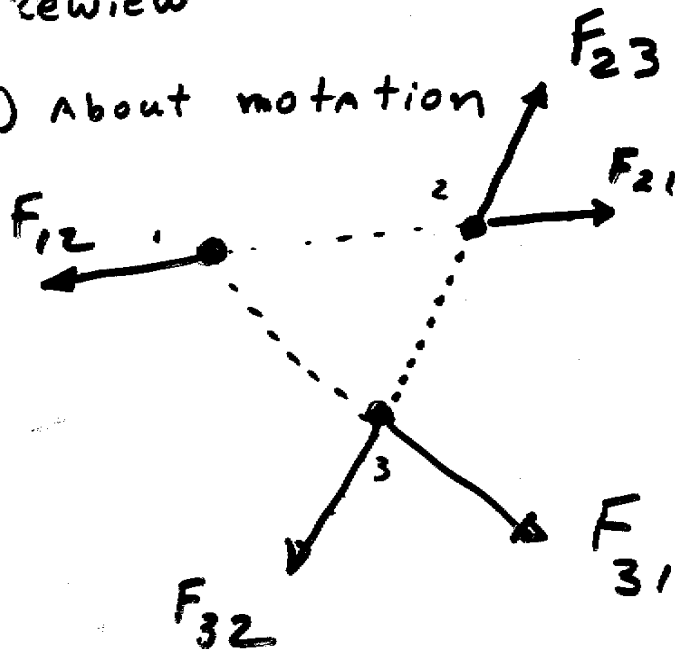
6

Smallest amount  
of charge in  
the world

$$e = 1.6 \times 10^{-19} \text{ C}$$

Review

1) About notation



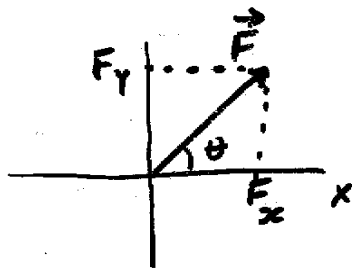
PROTON charge =  $e$

ELECTRON charge =  $-e$

How many protons  
will make  
1 coulomb?

ANSWER:  $N = 6.25 \times 10^{18}$

2) sin and cos



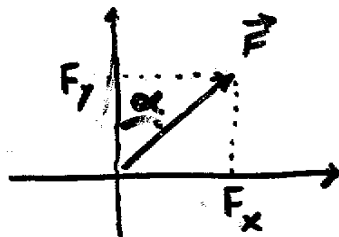
Horizontal component

$$F_x = F \cos \theta$$

Vertical component

$$F_y = F \sin \theta$$

Sometimes the angle is specified in a different way:

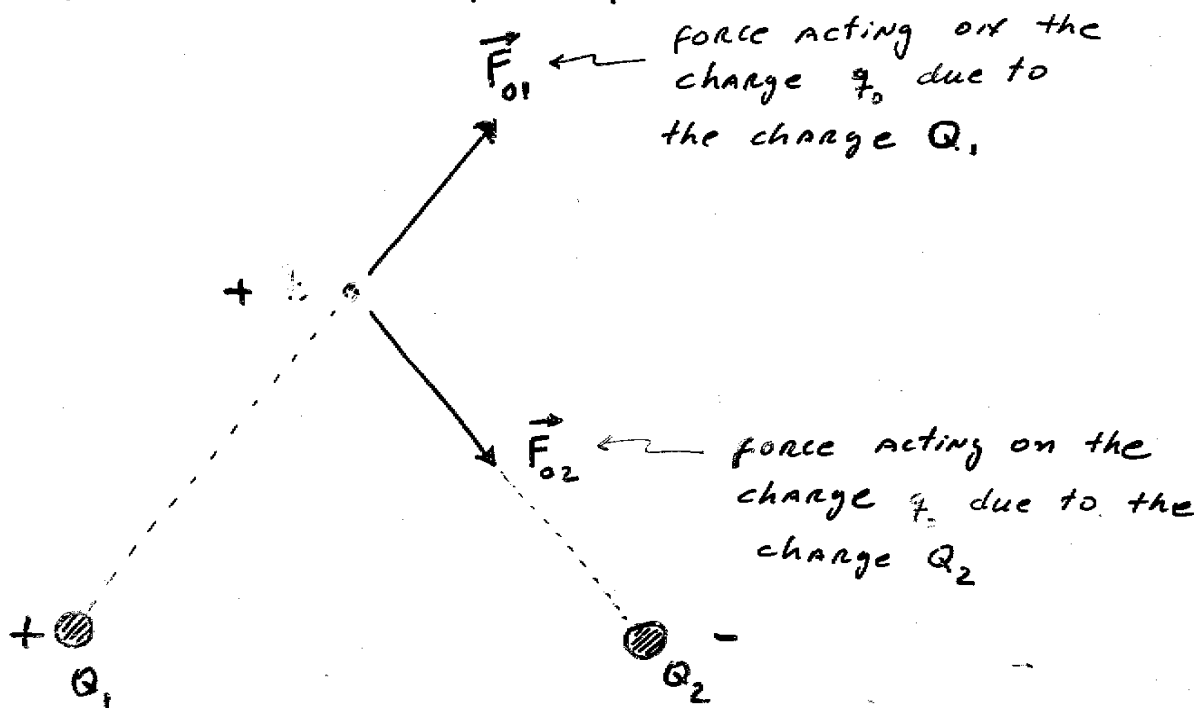


Horizontal component

$$F_x = F \sin \alpha$$

$$F_y = F \cos \alpha$$

## 3) Superposition principle

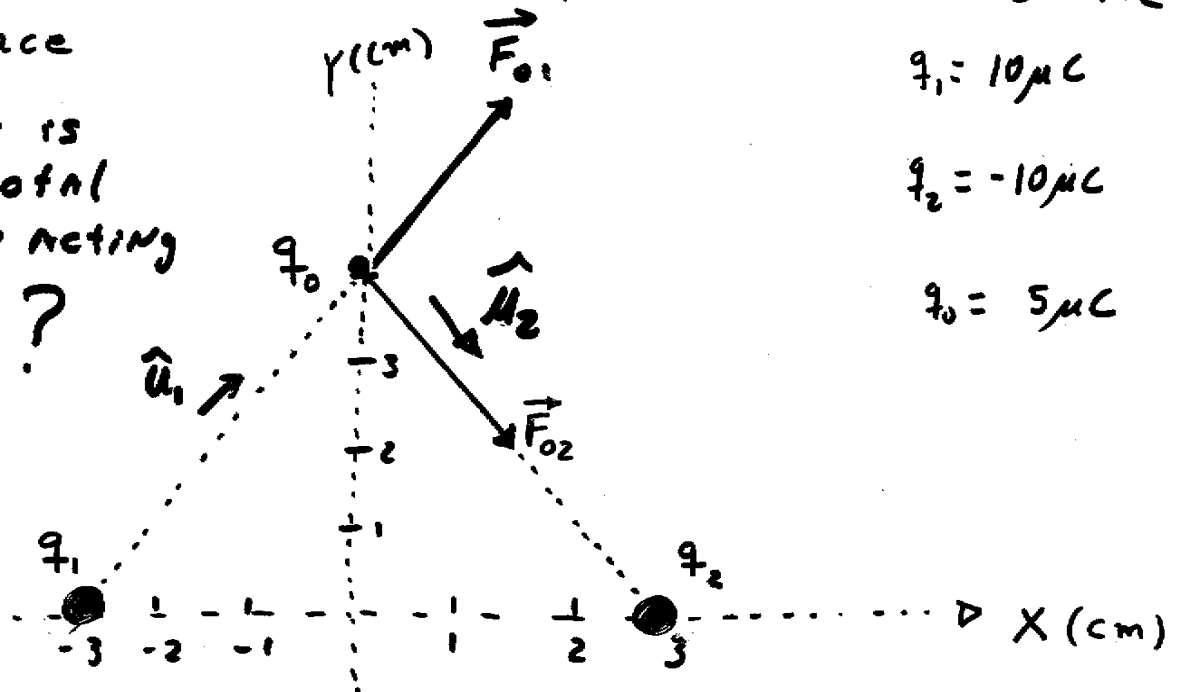


What is the total force acting on the charge  $q_0$ ?

$$\vec{F} = \vec{F}_{01} + \vec{F}_{02}$$

- 4) Instead of applying symmetry, we can always use a long method to find the electrostatic force

What is the total force acting on  $q_0$ ?

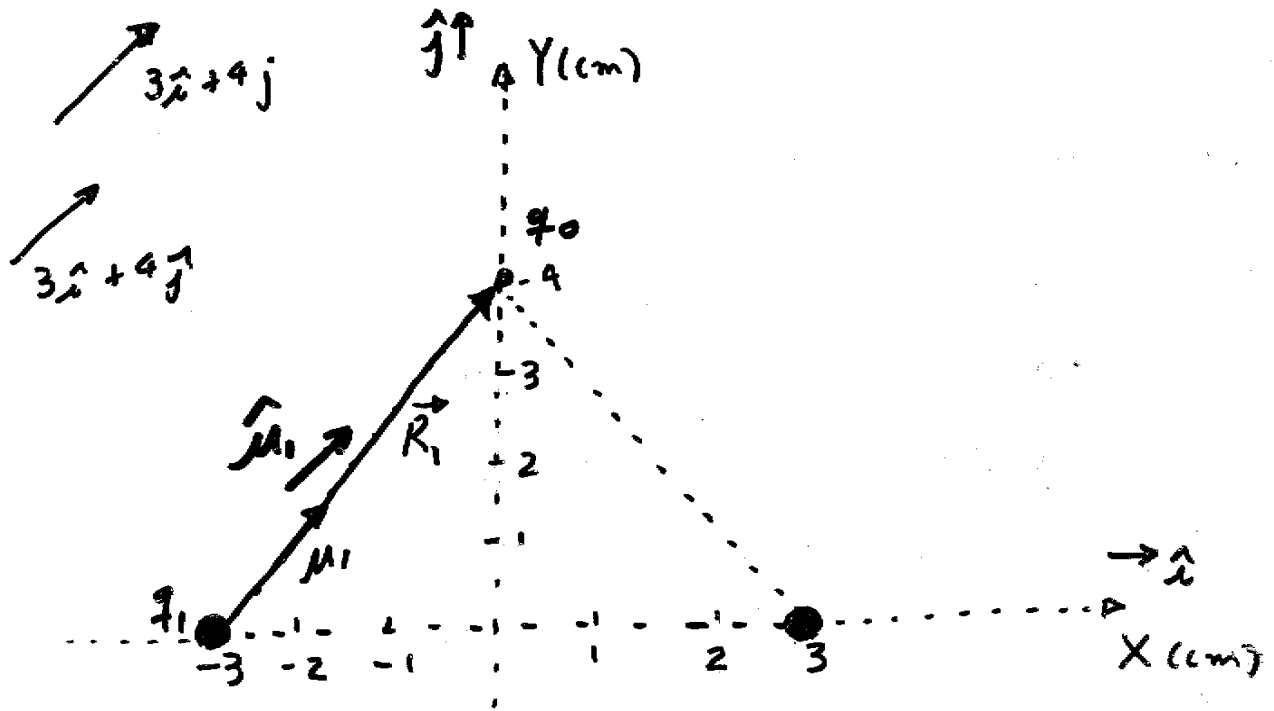


$$\vec{F}_{01} = \underbrace{F_{01}} \underbrace{\hat{u}_1}$$

magnitude

$$F_{01} = \frac{1}{4\pi\epsilon_0} \frac{|q_0||q_1|}{r^2} = 180 \text{ N}$$

9 How to find the proper unit vector :



Answer: Find any vector parallel to  $\hat{u}_1$   
and divide it by its magnitude

For example: let's take the vector  $\vec{R}_1$

$$\vec{R}_1 = 3\hat{i} + 4\hat{j}$$

$$|\vec{R}_1| = \sqrt{3^2 + 4^2} = 5 \text{ cm}$$

$$\hat{u}_1 = \frac{\vec{R}_1}{|\vec{R}_1|} = \frac{3}{5}\hat{i} + \frac{4}{5}\hat{j}$$

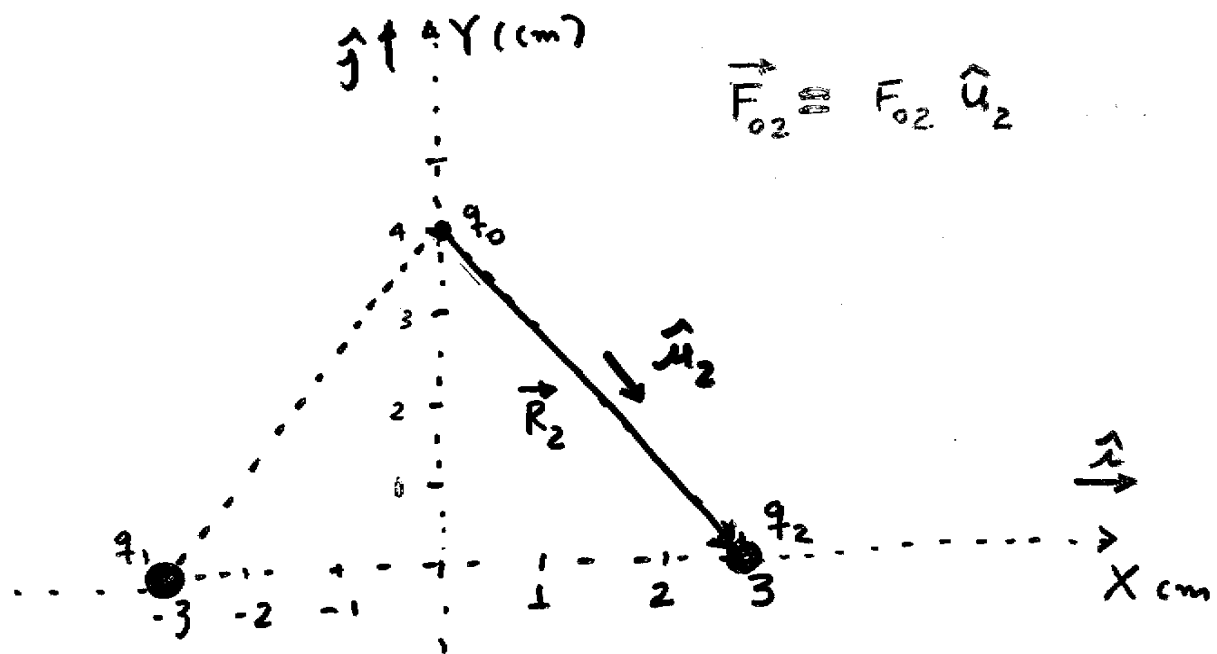
Therefore:

$$\vec{F}_{01} = F_{01} \vec{u}_1$$

$$= 180 \text{ Newtons} \times \left( \frac{3}{5} \hat{i} + \frac{4}{5} \hat{j} \right)$$

$$\vec{F}_{01} = 108 \hat{i} + 144 \hat{j} \quad (\text{in Newtons})$$

We apply the same procedure for  $\vec{F}_{02}$ :



How to find  $\hat{u}_2$ ?

$$\vec{R}_2 = 3\hat{i} - 4\hat{j} \quad \leftarrow R_2 \text{ is a vector that goes from the position of } q_0 \text{ toward the position of } q_2$$

$$|\vec{R}_2| = 5 \text{ cm}$$

$$\hat{u}_2 = \frac{\vec{R}_2}{|\vec{R}_2|} = \frac{3}{5}\hat{i} - \frac{4}{5}\hat{j}$$

$$\vec{F}_{02} = F_{02} \hat{u}_2 = 180 \left( \frac{3}{5}\hat{i} - \frac{4}{5}\hat{j} \right) \quad \text{in Newtons}$$

$$= 108\hat{i} - 144\hat{j}$$

42

$$\vec{F}_{01} = 180 \text{ N } \hat{u}_1 = 180 \text{ N} \left( \frac{3}{5} \hat{i} + \frac{4}{5} \hat{j} \right)$$

$$\vec{F}_{02} = 180 \text{ N } \hat{u}_2 = 180 \text{ N} \left( \frac{3}{5} \hat{i} - \frac{4}{5} \hat{j} \right)$$

---

$$\vec{F}_{01} + \vec{F}_{02} = 2 \times 180 \times \frac{3}{5} \hat{i}$$

Practice problem: QUESTION #7, Textbook page 517  
(such question is related to  
what we have done in class)

Read: sample problem 22-1 (page 511)

Practice questions: Q3, Q6 (page 517)

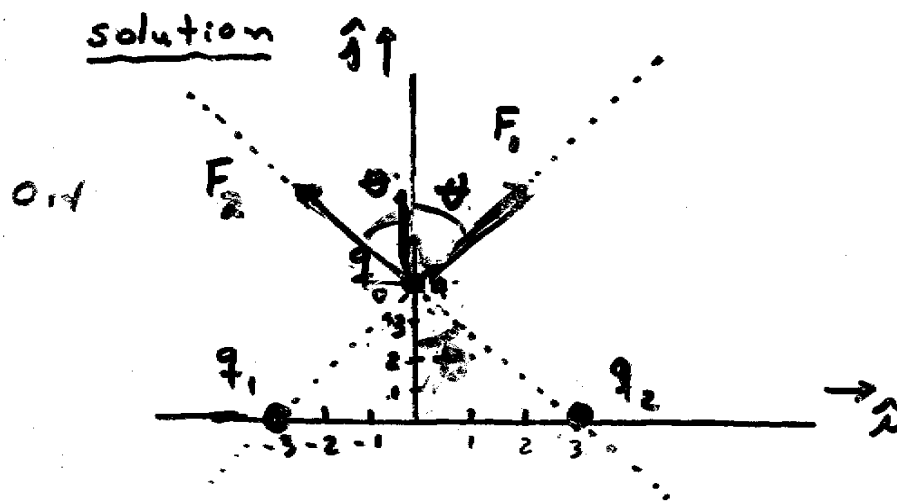
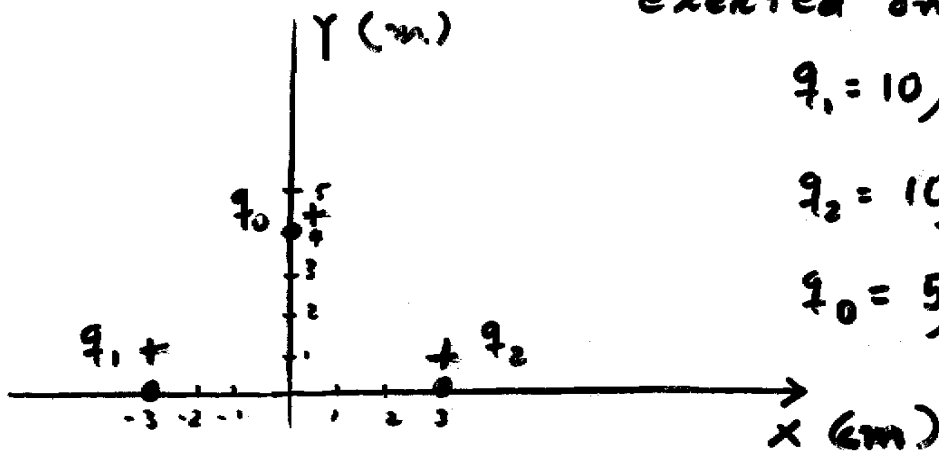
B

EXERCISE Find the electrostatic force exerted on charge  $q_0$ .

$$q_1 = 10 \mu\text{C}$$

$$q_2 = 10 \mu\text{C}$$

$$q_0 = 5 \mu\text{C}$$



Let's use symmetry

- Notice the horizontal components will cancel out
- So, let's calculate only the vertical component of each force  $\vec{F}_1$  and  $\vec{F}_2$

19

$$\underbrace{(F_2)_y}_{\substack{\uparrow \\ \text{vertical} \\ \text{component}}} = \underbrace{F_2}_{\substack{\uparrow \\ \text{magnitude of} \\ \text{the force } \vec{F}_2}} \cos \theta$$

$$F_2 = \left( \frac{1}{4\pi\epsilon_0} \right) \frac{q_2 q_0}{r^2} = 180$$

$$\cos \theta = \frac{4}{5}$$

$$9 \times 10^9 \times \frac{10 \times 10^{-6} \times 5 \times 10^{-6}}{(5 \times 10^{-2})^2}$$

$$= 180 \text{ N}$$

$$(\vec{F}_2)_y = F_2 \cos \theta = \frac{4}{5} \times 180 \text{ N} \leftarrow$$

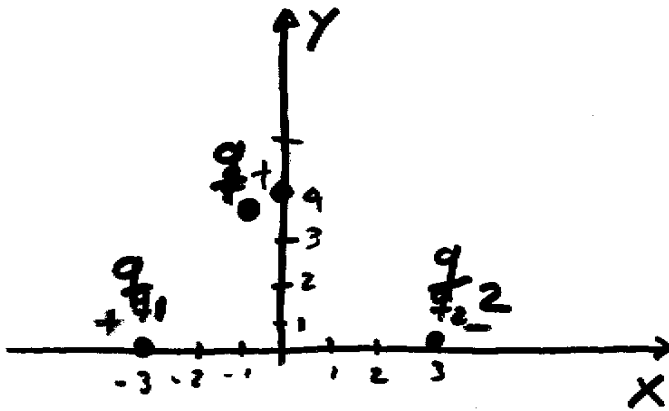
On the other hand

$$(\vec{F}_1)_y = \frac{4}{5} \times 180 \leftarrow$$

So, total force

$$\vec{F}_1 + \vec{F}_2 = \frac{8}{5} \times 180 \uparrow$$

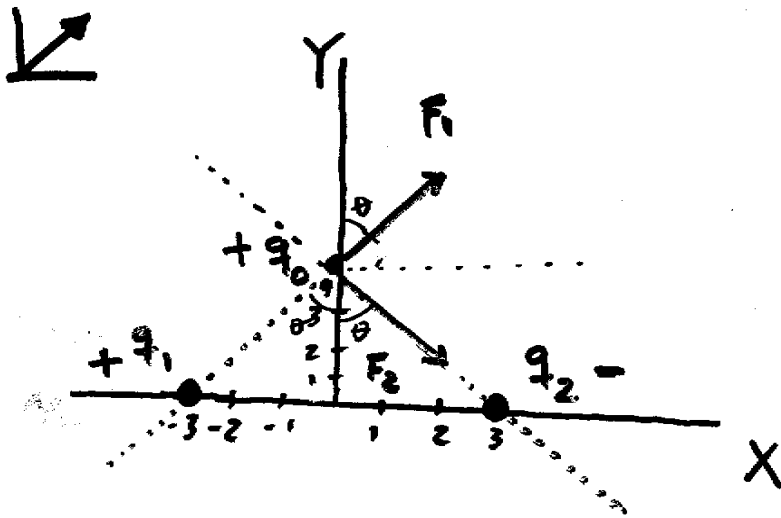
EXERCISE Find the electrostatic force created on charge  $q_0$



$$q_1 = 10 \mu\text{C}$$

$$q_2 = -10 \mu\text{C}$$

$$q_0 = 5 \mu\text{C}$$



- Notice the vertical component of  $\vec{F}_1$  will cancel out the vertical component of  $\vec{F}_2$
- So, let's calculate only the horizontal components

16

$$\underbrace{(\vec{F}_2)_x}_{\text{horizontal component}} = \underbrace{F_2}_{\text{magnitude of force } \vec{F}_2} \sin \theta$$

$$F_2 = \frac{1}{4\pi\epsilon_0} \frac{q_2 q_1}{r^2} =$$

$$\sin \theta =$$

$$(\vec{F}_2)_x = F_2 \sin \theta =$$

So, the total force

$$\vec{F}_1 + \vec{F}_2 = \dots$$

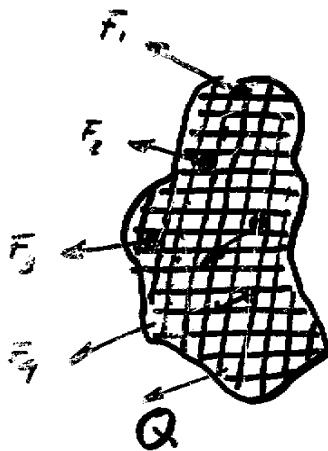
Reading assignment:

sample problem 22-2, page 512 textbook

TOTAL FORCE  
ON CHARGE Q?



•  
q

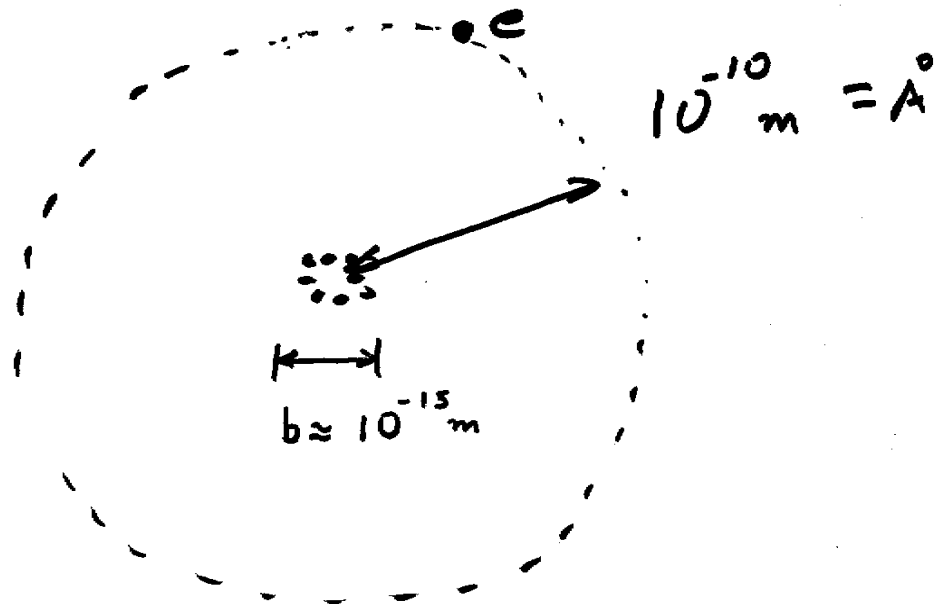


•  
q

$$F_{\text{Total}} = \vec{F}_1 + \vec{F}_2 + \vec{F}_3 + \dots$$

$$\sum_i \vec{F}_i$$

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Is this figure drawn on scale?

If  $b$  were the size of this classroom  
(this is, the classroom were the nucleus)

THEN

the outermost electron of the atom

would be at  $\quad \quad \quad$  km far away from us  
 $\quad \quad \quad$  miles

Answer: NO